

### Postulates, Theorems, and Corollaries Chapter 4



**Thm. 4-3-1 Triangle Sum Theorem** The sum of the angle measures of a triangle is  $180^\circ$ .

**Cor. 4-3-2** The acute angles of a right triangle are complementary.

**Cor. 4-3-3** The measure of each angle of an equiangular triangle is  $60^\circ$ .

**Thm. 4-3-4 Exterior Angle Theorem** The measure of an exterior angle of a triangle is equal to the sum of the measures of its remote interior angles.

**Thm. 4-3-5 Third Angles Theorem** If two angles of one triangle are congruent to two angles of another triangle, then the third pair of angles are congruent.

**Post. 4-5-1 Side-Side-Side (SSS) Congruence Postulate** If three sides of one triangle are congruent to three sides of another triangle, then the triangles are congruent.

**Post. 4-5-2 Side-Angle-Side (SAS) Congruence Postulate** If two sides and the included angle of one triangle are congruent to two sides and the included angle of another triangle, then the triangles are congruent.

**Post. 4-6-1 Angle-Side-Angle (ASA) Congruence Postulate** If two angles and the included side of one triangle are congruent to two angles and the included side of another triangle, then the triangles are congruent.

**Thm. 4-6-2 Angle-Angle-Side (AAS) Congruence Theorem** If two angles and a nonincluded side of one triangle are congruent to the corresponding angles and nonincluded side of another triangle, then the triangles are congruent.

**Thm. 4-6-3 Hypotenuse-Leg (HL) Congruence Theorem** If the hypotenuse and a leg of a right triangle are congruent to the hypotenuse and a leg of another right triangle, then the triangles are congruent.

**Thm. 4-9-1 Isosceles Triangle Theorem** If two sides of a triangle are congruent, then the angles opposite the sides are congruent.

**Thm. 4-9-2 Converse of the Isosceles Triangle Theorem** If two angles of a triangle are congruent, then the sides opposite those angles are congruent.

**Cor. 4-9-3** If a triangle is equilateral, then it is equiangular.

**Cor. 4-9-4** If a triangle is equiangular, then it is equilateral.

## Postulates, Theorems, and Corollaries Chapter 3



**Post. 3-2-1 Corresponding Angles Postulate** If two parallel lines are cut by a transversal, then the pairs of corresponding angles are congruent.

**Thm. 3-2-2 Alternate Interior Angles Theorem** If two parallel lines are cut by a transversal, then the pairs of alternate interior angles are congruent.

**Thm. 3-2-3 Alternate Exterior Angles Theorem** If two parallel lines are cut by a transversal, then the two pairs of alternate exterior angles are congruent.

**Thm. 3-2-4 Same-Side Interior Angles Theorem** If two parallel lines are cut by a transversal, then the two pairs of same-side interior angles are supplementary.

**Post. 3-3-1 Converse of the Corresponding Angles Postulate** If two coplanar lines are cut by a transversal so that a pair of corresponding angles are congruent, then the two lines are parallel.

**Post. 3-3-2 Parallel Postulate** Through a point  $P$  not on line  $\ell$ , there is exactly one line parallel to  $\ell$ .

**Thm. 3-3-3 Converse of the Alternate Interior Angles Theorem** If two coplanar lines are cut by a transversal so that a pair of alternate interior angles are congruent, then the two lines are parallel.

**Thm. 3-3-4 Converse of the Alternate Exterior Angles Theorem** If two coplanar lines are cut by a transversal so that a pair of alternate exterior angles are congruent, then the two lines are parallel.

**Thm. 3-3-5 Converse of the Same-Side Interior Angles Theorem** If two coplanar lines are cut by a transversal so that a pair of same-side interior angles are supplementary, then the two lines are parallel.

**Thm. 3-4-1** If two intersecting lines form a linear pair of congruent angles, then the lines are perpendicular.

**Thm. 3-4-2 Perpendicular Transversal Theorem** In a plane, if a transversal is perpendicular to one of two parallel lines, then it is perpendicular to the other line.

**Thm. 3-4-3** If two coplanar lines are perpendicular to the same line, then the two lines are parallel to each other.

**Thm. 3-5-1 Parallel Lines Theorem** In a coordinate plane, two nonvertical lines are parallel if and only if they have the same slope. Any two vertical lines are parallel.

**Thm. 3-5-2 Perpendicular Lines Theorem** In a coordinate plane, two nonvertical lines are perpendicular if and only if the product of their slopes is  $-1$ . Vertical and horizontal lines are perpendicular.

## Postulates, Theorems, and Corollaries Chapter 2



**Thm. 2-6-1 Linear Pair Theorem** If two angles form a linear pair, then they are supplementary.

**Thm. 2-6-2 Congruent Supplements Theorem** If two angles are supplementary to the same angle (or to two congruent angles), then the two angles are congruent.

**Thm. 2-6-3 Right Angle Congruence Theorem** All right angles are congruent.

**Thm. 2-6-4 Congruent Complements Theorem** If two angles are complementary to the same angle (or to two congruent angles), then the two angles are congruent.

**Thm. 2-7-1 Common Segments Theorem** Given collinear points  $A$ ,  $B$ ,  $C$ , and  $D$  arranged as shown, if  $\overline{AB} \cong \overline{CD}$ , then  $\overline{AC} \cong \overline{BD}$ .



**Thm. 2-7-2 Vertical Angles Theorem** Vertical angles are congruent.

**Thm. 2-7-3** If two congruent angles are supplementary, then each angle is a right angle.

## Postulates, Theorems, and Corollaries Chapter 1



**Post. 1-1-1** Through any two points there is exactly one line.

**Post. 1-1-2** Through any three noncollinear points there is exactly one plane containing them.

**Post. 1-1-3** If two points lie in a plane, then the line containing those points lies in the plane.

**Post. 1-1-4** If two lines intersect, then they intersect in exactly one point.

**Post. 1-1-5** If two planes intersect, then they intersect in exactly one line.

**Post. 1-2-1 Ruler Postulate** The points on a line can be put into a one-to-one correspondence with the real numbers.

**Post. 1-2-2 Segment Addition Postulate** If  $B$  is between  $A$  and  $C$ , then  $AB + BC = AC$ .

**Post. 1-3-1 Protractor Postulate** Given  $\overleftrightarrow{AB}$  and a point  $O$  on  $\overleftrightarrow{AB}$ , all rays that can be drawn from  $O$  can be put into a one-to-one correspondence with the real numbers from 0 to 180.

**Post. 1-3-2 Angle Addition Postulate** If  $S$  is in the interior of  $\angle PQR$ , then  $m\angle PQS + m\angle SQR = m\angle PQR$ .

**Thm. 1-6-1 Pythagorean Theorem** In a right triangle, the sum of the squares of the lengths of the legs is equal to the square of the length of the hypotenuse.